LIST OF SYMBOLS

We used the following notation throughout the thesis and will introduce additional notation when needed:

- S Schedule;
- *n* Number of Jobs;
- *m* Parallel machines;
- *i* Job index;
- *j* Machine index;
- *P* Non-negative constants;
- *a* Learning index;
- *d* The common due-date;
- d_i Due date of operation with respect to job *i*;
- r_i Release time of operation with respect to job *i*;
- p_j The normal processing time of job j, j = 1, 2, ..., n;
- p_{ij} Processing time of job *i* on machine *j*;
- d_{ii} Due date of job *i* on machine *j*;
- w_i Weight of job *i*;
- a_i The aging factor of job j, j = 1, 2, ..., n;

- Π All possible job Sequences;
- r_{ij} Release time of job *i* on machine *j*;
- d^* Optimal common due date;
- σ^* Optimal job sequence;
- C_i The completion time of job j, j = 1, 2, ..., n;
- E_j The earliness of job j, j = 1, 2, ..., n, i.e. $E_j = \max\{0, d C_j\};$
- T_j The tardiness of job j, j=1,2,...,n, i.e. $T_j = \max\{0, C_j d\};$
- t_i Due-date tolerance for job *i*;
- N_T Number of tardy jobs;
- C_{max} Makespan or total completion time;
- Idm Increasing series of dominating machines;
- ddm Decreasing series of dominating machines;