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References

Appendix A Plant and Control System Data
Appendix B Papers Published/Accepted for Publication


B3 Analysis of stabilised output error methods. Accepted for publication in IEE Proc of Control Theory and Applications, UK, 1995 Girija G and Raol J.R


* (Required to be included as per the guidelines of the BU)