

## APPENDIX

The pseudo spheroidal space-time metric derived in Chapter-2 has the form

$$ds^2 = e^{\nu(r)} dt^2 - \frac{1 + K \frac{r^2}{R^2}}{1 + \frac{r^2}{R^2}} dr^2 - r^2 d\theta^2 - r^2 \sin^2 \theta d\phi^2. \quad (\text{A.1})$$

The non-zero components of Ricci tensor and Ricci scalar for the metric (A.1) are given below.

$$R_{00} = - \frac{e^{\nu} \left(1 + \frac{r^2}{R^2}\right) \left[ \frac{\nu''}{2} + \frac{\nu'^2}{4} + \frac{\nu'}{r} - \frac{(K-1)r\nu'}{2R^2 \left(1 + \frac{r^2}{R^2}\right) \left(1 + K \frac{r^2}{R^2}\right)} \right]}{\left(1 + K \frac{r^2}{R^2}\right)}$$

$$R_{11} = \frac{\nu'}{2} + \frac{\nu'^2}{4} - \frac{(K-1)r\nu'}{2R^2 \left(1 + \frac{r^2}{R^2}\right) \left(1 + K \frac{r^2}{R^2}\right)} - \frac{2(K-1)}{R^2 \left(1 + \frac{r^2}{R^2}\right) \left(1 + K \frac{r^2}{R^2}\right)}$$

$$R_{22} = - \frac{\frac{r^2}{R^2}}{1 + K \frac{r^2}{R^2}} \left[ \frac{(K-1)}{1 + K \frac{r^2}{R^2}} + (K-1) \right] - \frac{r\nu'}{2 \left(1 + \frac{r^2}{R^2}\right) \left(1 + K \frac{r^2}{R^2}\right)^{-1}}$$

$$R_{33} = \sin^2 \theta R_{22}.$$

$$R = - \frac{1 + \frac{r^2}{R^2}}{1 + K \frac{r^2}{R^2}} \left[ \nu' + \frac{\nu'^2}{2} - \frac{[K-1]r\nu'}{R^2 \left(1 + \frac{r^2}{R^2}\right) \left(1 + K \frac{r^2}{R^2}\right)} \right] + \frac{4(K-1)}{R^2 \left(1 + K \frac{r^2}{R^2}\right)^2} + \frac{2(K-1)}{R^2 \left(1 + K \frac{r^2}{R^2}\right)} - \frac{2\nu'}{r \left(1 + K \frac{r^2}{R^2}\right)} \left(1 + \frac{r^2}{R^2}\right)$$

The surviving components of Einstein's tensor

$$G_i^j = R_i^j - \frac{1}{2} R \delta_i^j \text{ are given below.}$$

$$G_0^0 = \frac{-3(K-1) \left(1 + \frac{K}{3} \frac{r^2}{R^2}\right)}{R^2 \left(1 + K \frac{r^2}{R^2}\right)^2}$$

$$G_1^1 = \frac{\left(1 + \frac{r^2}{R^2}\right) \frac{v'}{r} - \frac{(K-1)}{R^2}}{\left(1 + K \frac{r^2}{R^2}\right)}$$

$$G_2^2 = \frac{1 + \frac{r^2}{R^2}}{1 + K \frac{r^2}{R^2}} \left[ \frac{v''}{2} + \frac{v'^2}{4} + \frac{v'}{2r} \right] - \frac{r(K-1)}{R^2} \frac{\left(\frac{v'}{2} + \frac{1}{r}\right)}{\left(1 + K \frac{r^2}{R^2}\right)^2}$$

$$G_3^3 = G_2^2.$$

The following are the components of the Weyl tensor.

$$\begin{aligned} C_{1212} &= \frac{r^2}{12} \left[ v'' + \frac{v'^2}{2} - \frac{(K-1)rv'}{R^2 \left(1 + \frac{r^2}{R^2}\right) \left(1 + K \frac{r^2}{R^2}\right)} - \frac{v'}{r} \right] - \frac{1}{6} \frac{K(K-1) \left(\frac{r^2}{R^2}\right)^2}{\left(1 + \frac{r^2}{R^2}\right) \left(1 + K \frac{r^2}{R^2}\right)} \\ &= \frac{C_{1313}}{\sin^2 \theta} \\ &= \frac{r^2 e^{-\nu}}{2} C_{1010} \end{aligned}$$

$$= - \frac{1 + K \frac{r^2}{R^2}}{2r^2 \left(1 + \frac{r^2}{R^2}\right) \sin^2 \theta} C_{2323}$$

$$= - \frac{1 + K \frac{r^2}{R^2}}{1 + \frac{r^2}{R^2}} e^{-\nu} C_{2020}$$

$$= - \frac{1 + K \frac{r^2}{R^2}}{\left(1 + \frac{r^2}{R^2}\right) \sin^2 \theta} e^{-\nu} C_{3030}$$