CHAPTER – III
MHD AND MIXED CONVECTION FLOW OF MAXWELL FLUID
ON HEAT TRANSFER NEAR A STAGNATION POINT FLOW
1. INTRODUCTION

The fluids like soups, shampoos, tomato paste, condensed milk, sugar solution, apple source, mud etc. cannot be described by the Newton's law of viscosity. Such fluids are known as the non-Newtonian fluids. The non-Newtonian fluids in view of their diverse rheological properties cannot be examined through one constitutive relationship between shear stress and rate of strain. Many models of non-Newtonian fluids exist. Maxwell model is one subclass of rate type fluids. This fluid model is especially useful for polymers of low molecular weight. In view of its simplicity, this fluid model has acquired special status amongst the recent workers in the field. For instance Wang and Tan [143] discussed the flow of Maxwell fluid in a porous medium. Exact solution of Helical flows of Maxwell fluid with shear stress on the boundary is addressed by Jamil and Fetecau [62]. Zierep and Fetecau [152] studied Rayleigh-Stokes problem using Maxwell fluid. Exact solution is constructed here. Numerical solution for stagnation point flow of Maxwell fluid was computed by Sadeghy et al. [47]. Megahed [90] studied the variable fluid properties and variable heat flux effects on the flow and heat transfer in a non-Newtonian Maxwell fluid over an unsteady stretching sheet with slip velocity. An exact solution for the stretching/shrinking wall problem in a viscous fluid was provided by Yao et al. [149].

The mixed convection flow occurs in several industrial and technical applications which include nuclear reactors cooled during emergency shutdown, electronics devices cooled by fans, heat exchangers placed in a low velocity environment, and solar central receivers exposed to wind currents. In the study of fluid over heated or cooled surfaces, it is customary to neglect the effect of the buoyancy forces when the flow is horizontal. However for vertical or inclined surfaces, the buoyancy force modifies the flow field and hence the heat transfer rate. Therefore, it is not possible to neglect the effect of buoyancy forces for vertical or inclined heated or cooled surfaces. In recent years, much attention has been paid to develop efficient energy systems. Many recent studies have been focused on the problem of magnetic field effect on laminar mixed convection boundary layer flow over a vertical non-linear stretching sheet [34, 50, 16].

The magnetohydrodynamic (MHD) problems of flow of an electrically conducting fluid over a stretching porous plate in a porous medium with an external transverse uniform magnetic field has many applications in petroleum industry,
purification of crude oil and fluid droplets sprays wire and fiber coating and polymer technology, production of plastic sheets and foils, and cold drawing of plastic sheets. All these processes depend on the physical/rheological properties of the fluid around the sheet. Many studies to understand the features of the flow over a stretching sheet had been done traditionally for Newtonian fluids, although the fluids used in industrial purposes are non-Newtonian. The MHD flow and heat transfer over a stretching sheet is one of the very important problems in fluid mechanics. It had been discussed for the first time by Sakiadis [118]. The concept of convective boundary conditions was initiated by Aziz [12]. He discussed the boundary layer flow of viscous fluid over a flat plate subject to convective surface condition. Makinde and Aziz [83] reported the influence of convective surface condition in MHD mixed convection flow from a vertical surface in a porous medium. The effect of Hall currents on flow and heat transfer over an unsteady stretching surface in the presence of a strong magnetic field has been analyzed by El-Aziz [42]. Bataller [17] studied the magnetohydrodynamic flow and heat transfer of an upper-convected Maxwell fluid due to a stretching sheet. Habibi Matin et al. [51] studied the mixed convection MHD flow of nanofluid over a non-linear stretching sheet with effects of viscous dissipation and variable magnetic field.

The radiative effects have important applications in physics and engineering particularly in space technology and high temperature processes [113]. Effects of radiation have been studied by Abdul Hakeem and Sathiyanathan [3], Seddeek and Abdelmeguid [124], Mamun Molla and Anwar Hossain [85], Hayat et al. [56] studied the mixed convection radiative flow of maxwell fluid near a stagnation point with convective condition. Soid et al. [129] studied the magnetohydrodynamics boundary layer flows over a stretching surface with radiation effect and embedded in porous medium.

The present study contains an analysis of the effects of mixed convective flow of a Maxwell fluid over a stretching sheet by taking MHD into account. Using the similarity transformations, the governing equations have been transformed into a set of ordinary differential equations, which are nonlinear and cannot be solved analytically, therefore, fourth order Runge-Kutta method along with shooting technique has been used for solving it. The results for velocity and temperature functions are carried out for the wide range of important parameters namely, magnetic
parameter, viscosity parameter, thermal conductivity parameter and radiation parameter. The skin friction and rate of heat transfer have also been computed.

2. MATHEMATICAL FORMULATION

Let us consider the two-dimensional mixed convection stagnation point flow of an incompressible and radiative Maxwell fluid near a stretched surface. The schematic diagram of physical model is shown in figs. A & B. The flow is in the region \( y > 0 \) and is subjected to a non-uniform magnetic field applied normally to the surface, \( B_0 \) is the initial strength of the magnetic field. It is assumed that the magnetic Reynolds number is very small and as there is no electric field, the electric field due to polarization of charges is neglected. Under these assumptions along with the Boussinesq and boundary layer approximations, the system of equations, which models the flow is given by

Continuity equation

\[
\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} = 0 \tag{2.1}
\]

Linear momentum equation

\[
u \frac{\partial u}{\partial x} + v \frac{\partial u}{\partial y} + \lambda \left[ u^2 \frac{\partial^2 u}{\partial x^2} + v^2 \frac{\partial^2 u}{\partial y^2} + 2uv \frac{\partial^2 u}{\partial x \partial y} \right] = u_e \frac{du_e}{dx} + v \frac{\partial^2 u}{\partial y^2} - \frac{\sigma B_0^2}{\rho} u + g \beta_r (T - T_\infty) \tag{2.2}
\]

Energy equation

\[
u \frac{\partial T}{\partial x} + v \frac{\partial T}{\partial y} = \frac{1}{\rho c_p} \frac{\partial}{\partial y} \left( \kappa \frac{\partial T}{\partial y} \right) - \frac{\partial q_r}{\partial y} \tag{2.3}
\]

The boundary conditions for the velocity, temperature and concentration fields are

\[
u = u_e (x) = cx, \quad v = 0, \quad -k \frac{\partial T}{\partial y} = h(T_y - T) \quad \text{at} \quad y = 0
\]

\[
u = u_e (x) = ax, \quad T \to T_\infty \quad \text{as} \quad y \to \infty \tag{2.4}
\]

where \( u \) and \( v \) are the velocity components along \( x \) and \( y \) directions, respectively, \( \rho \) is the fluid density, \( T \) is the temperature of the fluid, \( \lambda \) is the relaxation time, \( c_p \) is the specific heat at constant pressure, \( \mu \) is the fluid viscosity, \( k \) is the fluid thermal
conductivity, \( T_\infty \) is the free stream temperature and \( T_f \) is the convective fluid temperature.

By using the Rosseland approximation the radiative heat flux \( q_r \) is given by

\[
q_r = -\frac{4\sigma^* k^*}{3k^*} \frac{\partial T^4}{\partial y} \tag{2.5}
\]

Where \( \sigma^* \) is the Stefan-Boltzmann constant and \( k^* \) is the mean absorption coefficient. It should be noted that by using the Rosseland approximation, the present analysis is limited to optically thick fluids. If temperature differences within the flow are significantly small, then equation [2.5] can be linearised by expanding \( T^4 \) into the Taylor series about \( T_\infty \), which after neglect higher order terms takes the form:
\[ T^4 \approx 4T_x^3T - 3T_x^4 \]  
(2.6)

In view of equations (2.5) and (2.6), eqn. (2.3) reduces to
\[ u \frac{\partial T}{\partial x} + v \frac{\partial T}{\partial y} = \alpha \frac{\partial^2 T}{\partial y^2} + \frac{16\sigma T_x^3}{3k \rho c_p} \frac{\partial^2 T}{\partial y^2} \]  
(2.7)

The continuity equation (2.1) is satisfied by the Cauchy Riemann equations
\[ u = \frac{\partial \psi}{\partial y} \quad \text{and} \quad v = -\frac{\partial \psi}{\partial x} \]  
(2.8)

where \( \psi(x, y) \) is the stream function.

In order to transform equations (2.2) and (2.7) into a set of ordinary differential equations, the following similarity transformations and dimensionless variables are introduced.

\[ \psi = \sqrt{ycxf(\eta)}, \eta = y\sqrt{c/v}, u = cxf'(\eta), v = -\sqrt{c/v}f(\eta) \]

\[ \theta(\eta) = \frac{T-T_e}{T_x-T_e}, \alpha = \frac{a}{c}, \beta = \lambda c, R = \frac{4\sigma T_x^3}{k^2 \rho c_p}, \lambda = \frac{Gr_x}{Re_x^2} \]  
(2.9)

\[ M = \frac{\sigma B_0^2}{\rho c}, Gr_x = \frac{g \beta_T(T_w-T_x)x^3}{v^2}, Pr = \frac{v}{\alpha} \]

where \( f(\eta) \) is the dimensionless stream function, \( \theta \) - dimensionless temperature, \( \eta \) - similarity variable, \( M \) - Magnetic parameter, \( a \) and \( c \) are constants, \( \beta \) - Deborah number, \( \lambda \) - mixed convection parameter, \( \alpha \) - ratio of rate constant, \( Gr_x \) - Grashof number, \( Re_x \) - Reynolds number, \( R \) - radiation parameter, \( Pr \) - Prandtl number.

In view of Equations (2.8) - (2.9), the Equations (2.2) and (2.7) transform into
\[ f'''' + ff'' - f'^2 + \alpha^2 - Mf' - \beta (f^2 f''' - 2ff' f'') + \lambda \theta = 0 \]  
(2.10)

\[ \left(1 + \frac{4}{3} R\right) \theta'' + Pr \ f \theta' = 0 \]  
(2.11)

The corresponding boundary conditions are:
\[ f(0) = 0, f'(0) = 1, \theta'(0) = -\gamma (1-\theta(0)) \]
\[ f'(\infty) = \alpha, \theta(\infty) = 0 \]  
(2.12)

where the primes denote differentiation with respect to \( \eta \).
The physical quantities of interest are the skin friction coefficient $C_f$, the local Nusselt number $Nu$ which are defined as

$$C_f = -2\Re_x^{-1/2} f''(0), \quad Nu = -\Re_x^{1/2} \theta'(0)$$

(2.13)

3 SOLUTION OF THE PROBLEM

The set of coupled non-linear governing boundary layer equations (2.10) and (2.11) together with the boundary conditions (2.12) are solved numerically by using Runge-Kutta fourth order technique along with shooting method. First of all, higher order non-linear differential Equations (2.10) and (2.11) are converted into simultaneous linear differential equations of first order and they are further transformed into initial value problem by applying the shooting technique (Jain et al.[61]). The resultant initial value problem is solved by employing Runge-Kutta fourth order technique. The step size $\Delta \eta = 0.05$ is used to obtain the numerical solution with five decimal place accuracy as the criterion of convergence. From the process of numerical computation, the skin-friction coefficient and Nusselt number, which are respectively proportional to $f''(0)$ and $-\theta'(0)$, are also sorted out and their numerical values are presented in a tabular form.

4 RESULTS AND DISCUSSION

The governing equations (2.10) - (2.11) subject to the boundary conditions (2.12) are integrated as described in section 3. In order to get a clear insight of the physical problem, the velocity and temperature have been discussed by assigning numerical values to the parameters encountered in the problem. The effects of various parameters on velocity profiles in the boundary layer are depicted in Figs. 1-7. The effects of various parameters on temperature profiles in the boundary layer are depicted in Figs. 8-13.

Fig. 1 shows the variation of the velocity with the viscosity parameter ($\alpha$). It is noticed that the velocity increases with an increase in the viscosity parameter. Fig. 2 shows the variation of the velocity with the Deborah number ($\beta$). It is noticed that the velocity decreases with an increase in the Deborah number. Fig. 3 illustrates the effect of the convective parameter ($\gamma$) on the velocity. It is seen that as the convective
parameter increases, the velocity increases. Fig. 4 shows the dimensionless velocity profiles for different values of magnetic parameter \((M)\). It is seen that, as expected, the velocity decreases with an increase of magnetic parameter. The magnetic parameter is found to retard the velocity at all points of the flow field. It is because that the application of transverse magnetic field will result in a resistive type force (Lorentz force) similar to drag force which tends to resist the fluid flow and thus reducing its velocity. Also, the boundary layer thickness decreases with an increase in the magnetic parameter. Fig. 5 illustrates the effect of the mixed convection parameter \((\lambda)\) on the velocity. It is seen that as the mixed convection parameter increases, the velocity increases. Fig. 6 shows the variation of the velocity with the Prandtl number \((Pr)\). It is noticed that the velocity decreases with an increase in the Prandtl number. Fig. 7 shows the variation of the velocity with the radiation parameter \((R)\). It is noticed that the velocity thickness increases with an increase in the radiation parameter.

Fig. 8 depicts the thermal boundary-layer with the viscosity parameter. It is noticed that the thermal boundary layer thickness decreases with an increase in the viscosity parameter. Fig. 9 depicts the thermal boundary-layer with the convective parameter. It is noticed that the thermal boundary layer thickness increases with an increase in the convective parameter. Fig. 10 shows the variation of the thermal boundary-layer with the magnetic parameter. It is observed that the thermal boundary layer thickness increases with an increase in the magnetic parameter. Fig. 11 illustrates the effect of the mixed convection parameter on the temperature. It is noticed that as the mixed convection parameter increases, the temperature decreases. Fig. 12 shows the variation of the thermal boundary-layer with the Prandtl number. It is noticed that the thermal boundary layer thickness decreases with an increase in the Prandtl number. Fig. 13 shows the variation of the thermal boundary-layer with the radiation parameter. It is observed that the thermal boundary layer thickness increases with an increase in the radiation parameter.

Table 1 show the variation of the skin friction and Nusselt number with for different values of \(a, \beta, \gamma, M, \lambda, R\) and \(Pr\). It is noticed that the skin friction increases where as Nusselt number decrease with an increase in the Deborah number or Magnetic parameter. It is found that the skin friction decreases where as Nusselt number increase with an increase in the viscosity parameter or convective parameter or mixed convective parameter. It is observed that both the skin friction and Nusselt
number increases with an increase in the Prandtl number and both the skin friction and Nusselt number decreases with an increase in the radiation parameter. The correctness of the present numerical method is checked with the results obtained by Pop et al. [111], Mahapatra and Gupta [80] and Hayat et al. [20] for the values of Skin friction coefficient in the limiting condition. Thus, it is seen from Table 2.

5 CONCLUSIONS

The effects of thermal radiation and heat transfer of a Maxwell fluid near a mixed convection stagnation point flow over a moving surface in the presence of MHD has been studied. The governing equations are approximated to a system of non-linear ordinary differential equations by similarity transformation. Numerical calculations are carried out for various values of the dimensionless parameters of the problem. It has been found that

1. The velocity decreases as well as temperature increases with an increase in the magnetic parameter.
2. The velocity and temperature decreases with an increase in the Prandtl parameter.
3. The skin friction reduces the viscosity parameter or convective parameter or mixed convective parameter or radiation parameter and increases with the Magnetic parameter or Deborah number or Prandtl number.
4. The Nusselt number reduces the Deborah number or magnetic parameter or radiation parameter and increases with the viscosity parameter or convective parameter.
Fig. 1 Velocity profiles for different values of $\alpha$

$M=1, \beta=0.3, \lambda=R=0.5, Pr=0.7$

$\alpha=0.1$
$\alpha=0.2$
$\alpha=0.3$
$\alpha=0.4$

Fig. 2 Velocity profiles for different values of $\beta$

$\alpha=0.2, M=0.5, \lambda=\gamma=R=0.5, Pr=0.7$

$\beta=0.0$
$\beta=0.5$
$\beta=1.0$
Fig. 3 Velocity profiles for different values of $\gamma$

Fig. 4 Velocity profiles for different values of $M$

\[
\alpha = 0.2, \beta = 0.1, M = 0.5, \lambda = R = 0.5, Pr = 0.7
\]
Fig. 5 Velocity profiles for different values of $\lambda$

$\alpha = 0.2, \beta = 0.1, M = 0.5, R = 0.5, \gamma = 0.5, Pr = 0.7$

- $\lambda = 0.5$
- $\lambda = 1.0$
- $\lambda = 1.5$

Fig. 6 Velocity for different values of $Pr$

$\alpha = 0.2, M = 0.5, \beta = 0.1, \lambda = R = \gamma = 0.5,$

- $Pr = 0.7$
- $Pr = 3.0$
- $Pr = 5.0$

Fig. 6 Velocity for different values of $Pr$
Fig. 7 Velocity profiles for different values of $R$

Fig. 8 Temperature for different values of $\alpha$

$\alpha=0.2, \ M=0.5, \ \beta=0.1, \ \lambda=\gamma=0.5, \ \text{Pr}=0.7$

$\beta=0.1, \ M=0.5, \ \lambda=\gamma=R=0.5, \ \text{Pr}=0.7$
Fig. 9 Temperature for different values of $\gamma$

$\alpha=0.2$, $\beta=0.1$, $M=0.5$, $\lambda=R=0.5$, $Pr=0.7$

Fig. 10 Temperature for different values of $M$

$\alpha=0.2$, $\beta=0.1$, $\lambda=R=0.5$, $Pr=0.7$
Fig.11 Temperature for different values of $\lambda$

Fig.12 Temperature for different values of $Pr$

\[ \alpha=0.2, \ \beta=0.1, \ \gamma=R=0.5, \ Pr=0.7 \]
Fig. 13 Temperature for different values of $R$

$\alpha=0.2, \ \beta=0.1, \ M=0.5, \ \gamma=0.5, \ Pr=0.7$

- $R=0.0$
- $R=0.6$
- $R=1.2$

$\eta$
Table 1 Numerical values of \(-f''(0), -\theta'(0)\) at the sheet for different values of \(\alpha, \beta, \gamma, M, \lambda, R\) and \(Pr\).

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Table 2 Numerical values of $f''(0)$ at the sheet for different values of $\lambda$, Comparison of the present results with that of Pop et al. [91], Mahapatra and Gupta [66] and Hayet et al.[50]

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