

APPENDIX A

THE ORTHONORMAL POLYNOMIALS RELATED TO THE EIGENVALUE DENSITY

In this appendix we give the expression for the orthonormal polynomials defined in eq.(2.2-2) of chapter II, for any arbitrary order ν . It is given by

$$[D_\nu D_{\nu-1}]^{1/2} P_\nu(x) = \begin{vmatrix} 1 & M_1 & M_2 & M_3 & \dots & M_\nu \\ M_1 & M_2 & M_3 & \dots & \dots & M_{\nu+1} \\ \dots & \dots & \dots & \dots & \dots & \dots \\ M_{\nu-1} & \dots & \dots & \dots & \dots & M_{2\nu-1} \\ 1 & x & x^2 & \dots & \dots & x^\nu \end{vmatrix} \quad (\text{A-1})$$

where D_ν is the determinant with the last row replaced by $[M_\nu, M_{\nu+1}, \dots, M_{2\nu}]$. The number of polynomials is the same as the dimension of the space. When the density is Gaussian, i.e.

$$\rho(x) = (2\pi\sigma^2)^{-1/2} \exp \left[-\frac{1}{2} \left(\frac{x-\epsilon}{\sigma} \right)^2 \right] \quad (\text{A-2})$$

the polynomials $P_\mu(x)$ are related to the Hermite polynomials $H_{e\mu}$ by

$$P_\mu(x) = (\mu!)^{-1/2} H_\mu \left[\frac{x-\epsilon}{\sigma} \right] \quad (\text{A-3})$$

$$\text{where } H_{e\mu}(x) = 2^{-\mu/2} H_\mu(x/\sqrt{2})$$

When the density is of Chi-squared type, the $P_\mu(x)$ are related to the Laguerre polynomials.