Chapter 4

A Customer Retention Model to Compare Rural and Urban Stores

4.1 Introduction

The term customer retention is the probability of a customer being “alive” or “repeat” buying from a firm (Gupta and Zeithams, 2006). Oliver (1997) define customer retention is deeply held commitment to re-buy or repatronize preferred product or service consistently in the future, despite situational influences and marketing efforts having the potential to cause switching behavior. Every business needs to survive, so it undertakes every possible action to get them. According to Drucker (1973), the main purpose of a business is to create a customer. Marketing has traditionally focused on market share and the customer acquisition rather than on retaining existing customers and on building long lasting relationships with them (Kotler, 2002). Gupta et al (2004) found that a one percent increase in customer retention had almost five times more impact on firm value than a one percent change in discount rate or cost of capital. Kotler and Keller (2006) give a reason for popularity of customer retention is the recognition that losing a customer means in fact more than a single sale i.e. losing the entire stream of purchases that this particular customer would make over a lifetime of patronage (Kotler and Keller, 2006).
The significance of customer retention was first introduced by Reichhel and Sasser (1990). They found that profits in service industries and credit card companies increased in direct proportion to the length of customer retention.

It is obvious that customer retention is more economical to keep existing customers than to acquire new one customer. Reichheld and Kenny (1990) observed that acquiring new customers is calculated as being five times more costly than the expenses of retaining existing customers. They observed that, long term customers buy more. The companies can clearly benefit from the life time spending of customers (Kotler, 2002 and Payne, 2006).

In literature the concept of customer retention and customer loyalty is treated as same. But Cohen et al (2006) argue that customer loyalty and customer retention are not same. According to Cohen et al (2006) consumer inertia implies that some customers are only being retained, rather than expressing loyalty. According to them customer loyal are described as being less price sensitive and more inclined to increase the number of purchase.

Dwyer (1997) and Jain and Singh (2002) observed that customer retention model exist for two classes “lost for good” and “always a share”. The “lost for good” class define as customer defection as permanent while the “always a share” class considers customer switching to competitors as transient. Kalbfleisch and Prentice (1980) used hazard models using which fall into broad groups- accelerated failure time (AFT) or proportional hazard (PH) models. Schmitten, Morrison and Colombo (1987) and Schmittlein and Peterson (1994) proposed a NBD/Pareto model for assessing the probability that a customer is still alive. This
model is used by Reinartz and Kumar (2000). Fader, Hardie and Lee (2005) modified this model. The “always share” retention models view customer switching to competitors and typically uses migration or Markov models to estimate transition probabilities of customers being in a certain state. Bitran and Mondschein (1996), Gonul and Shi (1998) and Pfeifer and Carraway (2000) defined these states based on RFM measures while Rust, Lemon and Zeithaml (2004) used brands as states and estimated transition probabilities using a logit model. Simester, Sun and Tsitsiklis (2005) used a binary tree approach to define the state space and estimated the transition probabilities using a non parametric approach. As mentioned earlier, retention are categorized into two groups- lost for good and always share. Some researchers have argued that customers should be treated as renewable resource (Dreze and Bonfrer, 2005). Thomas, Blattberg and Fox (2004) build a model for recapturing the lost customers.

4.2 Objective of this Chapter

The main objective of this chapter is to compare the customer retention of the grocery store for the two population i.e. rural and urban using stochastic model. The reason is that urban and rural customers are different in their culture, nature and purchasing capacity.

4.3 Hypotheses of this Chapter

Based on the objective our the major hypothesis is as follows

H$_0$: There is no significant difference between the ‘Customer retention’ of the grocery store of rural and urban.
Probabilistic model is used to compare the customer retention of rural and urban grocery store.

## 4.4 Data Collection

The sampling scheme and method of data collection for the application of customer retention model follows the discussion provided section 1.9 of chapter 1.

## 4.5 Methodology

The methodology adopted in the study can be used for comparing the customer retention of the grocery store for rural and urban population. For the purpose of comparison the investigator has to contact the respondents for three purchase occasion after a gap of three months. This is done to observe whether the respondent choice the grocery store at subsequent purchase occasions. Similarly, the investigator observed the same for the next purchase occasion. Now this makes sense to discuss the customer retention. The retention rate for the period $t$, denoted by $r_t$ is defined as follows

$$r_t = \frac{\text{Customer active at the end of the period } t}{\text{Customer active at the end of the period } t-1}$$

i.e. proportion of customers active at the end of period $t-1$ who are still active at the end of the period $t$.

Marketers particularly give importance to the concept for characterizing the distribution of customer life time. The distribution of customer life time is studied by the survivor function which is denoted by $S(t)$. The survivor function
is defined as the probability that a customer has survived to time “t” i.e. the customer is still active at the period “t”. The survival function $S(t)$ is defined as follows:

$$S(t) = \text{Probability that a customer survival up to time } t = r_1 \times r_2 \times ... \times r_t = \prod_{i=1}^{t} r_i$$

...(4.1)

Again,

$$S(t - 1) = \prod_{i=1}^{t-1} r_i$$

Thus,

$$r_t = \frac{S(t)}{S(t-1)}$$

...(4.2)

But practically it is observed that time horizon is limited and it is not possible to observe a cohort of customers infinitely. The investigator observed it is for some fixed time.

### 4.6 Introducing the Discrete Time Model

According to Fader and Hardie (2005), the duration of customer life times is based on the following two assumptions:

(i) Every customer has a constant retention probability “$1 - \theta$”. The duration of the customer’s relationship with the grocery store denoted by the random variable $T$. So, $T$ follows (shifted) geometric distribution with probability mass function
\[ p(T = t | \theta) = \theta (1 - \theta)^{t-1}; \quad t=1,2,3,... \] ... (4.3)

And survivor function is given by

\[ S(T = t | \theta) = (1 - \theta)^{t-1}; \quad t=1,2,3,... \] ... (4.4)

(ii) However, \( \theta \) cannot be considered as a constant but shall vary from customer to customer. Thus \( \theta \) is assumed to probability density function

\[ f(\theta | \alpha, \beta) = \frac{\theta^{a-1}(1-\theta)^{b-1}}{B(\alpha, \beta)}; \quad 0 < \theta < 1; \quad \alpha > 0, \beta > 0 \] ... (4.5)

The reason to take heterogeneity coefficient \( \theta \) to follow the beta distribution is for the flexibility of the distribution and also as it is bounded between zero and one. If both the parameters of the beta distribution \( (\alpha \text{ and } \beta) \) are small i.e. \( (\alpha, \beta < 1) \) the \( f(\theta | \alpha, \beta) \) is “U- Shaped” or highly polarized across the customers. If both the parameters are relatively large \( (\alpha, \beta > 1) \); then \( f(\theta | \alpha, \beta) \) are fairly homogeneous. The different shapes of the beta curve for different values of \( \alpha \text{ and } \beta \) can be seen in the figure 4.1
Figure 4.1 Beta Density Curves for Different Combination of the Values of the Parameters
Since $\theta$ is unobserved, i.e. for a given individual the value of $\theta$ shall remain constant over the time period of the study,

\[
P(T = t \mid \alpha, \beta) = \int_{0}^{1} P(T = t \mid \theta) f(\theta \mid \alpha, \beta) d\theta
\]

\[
= \int_{0}^{1} \theta (1 - \theta)^{t-1} \frac{\theta^{\alpha-1} (1 - \theta)^{\beta-1}}{B(\alpha, \beta)} d\theta
\]

\[
= \frac{1}{B(\alpha, \beta)} \int_{0}^{1} \theta^\alpha (1 - \theta)^{\beta+t-2} d\theta
\]

\[
= \frac{B(\alpha + 1, \beta + t - 1)}{B(\alpha, \beta)}
\]

... (4.6)

This forward recursion formula used to compute the probabilities is derived by the following manner

If we put $T = 1$ in (4.6) then

\[
P(T = 1 \mid \alpha, \beta) = \frac{B(\alpha + 1, \beta)}{B(\alpha, \beta)}
\]

\[
= \frac{\alpha}{\alpha + \beta}
\]

Now for $T = 2, 3 \ldots$

\[
P(T = t) = \frac{P(T = t)}{P(T = t - 1)} \times P(T = t - 1)
\]

\[
\Rightarrow \frac{P(T = t)}{P(T = t - 1)} = \frac{B(\alpha + 1, \beta + t - 1)}{B(\alpha, \beta)} \times \frac{B(\alpha, \beta)}{B(\alpha + 1, \beta + t - 2)}
\]

\[
= \frac{B(\alpha + 1, \beta + t - 1)}{B(\alpha + 1, \beta + t - 2)} = \frac{\beta + t - 2}{\alpha + \beta + t - 1}
\]
Finally, the customer retention rate is obtained using equation number (4.2). Substitute shifted Beta Geometric survivor function into (4.2) gives,

\[
R_t = \frac{S(t)}{S(t-1)}
\]

\[
= \frac{B(\alpha, \beta + t)}{B(\alpha, \beta + t - 1)}
\]

\[
= \frac{\beta + t - 1}{\alpha + \beta + t - 1}
\]

### 4.7 Estimation of the Parameters

The aim of this section is to compute the sBG model parameters using maximum likelihood estimate. Let, there are \( n_{u_t} \) and \( n_{r_t} \) customers who are still active at time \( t \) in grocery store for urban and rural population respectively. This means number of customer who buys products from the same store for the consecutive purchase occasion under study. Now, \( n_{u_1} \) and \( n_{r_1} \) are the urban and rural customer who drop out in the first period. Similarly, \( n_{u_2} \) and \( n_{r_2} \) are urban and rural customer who drop out in the second period. After the end of the second period, there are \( n_u - (n_{u_1} - n_{u_2}) \) and \( n_r - (n_{r_1} - n_{r_2}) \) customer still being active at the end of the second period for urban and rural population respectively. Assume that one customer is drop out is independent of the behavior of the other customer. It gives the specific values of the model parameter \( \alpha \) and \( \beta \). The joint probability of \( n_{u_1} \) and \( n_{u_2} \) urban customer and \( n_u - (n_{u_1} - n_{u_2}) \) urban customers still being active at the end of the second period is given by
\[ P(Data_u|\alpha, \beta) = P(T = 1|\alpha, \beta)^{n_{u1}} \times P(T = 2|\alpha, \beta)^{n_{u2}} \times S(2|\alpha, \beta)^{n_u - (n_{u1} - n_{u2})} \]

Similarly for rural,

\[ P(Data_r|\alpha, \beta) = P(T = 1|\alpha, \beta)^{n_{r1}} \times P(T = 2|\alpha, \beta)^{n_{r2}} \times S(2|\alpha, \beta)^{n_r - (n_{r1} - n_{r2})} \]

To estimate the model parameters, maximum likelihood estimation is used. So, the likelihood function is given by,

\[ L(\alpha, \beta|Data_u) = P(T = 1|\alpha, \beta)^{n_{u1}} \times P(T = 2|\alpha, \beta)^{n_{u2}} \times S(2|\alpha, \beta)^{n_u - (n_{u1} - n_{u2})} \]

Taking Log both side,

\[ LL(\alpha, \beta|Data_u) \]
\[ = n_{u1} \ln[p(T = 1|\alpha, \beta)] + n_{u2} \ln[p(T = 2|\alpha, \beta)] + [n_u - (n_{u1} + n_{u2})] \ln[S(2|\alpha, \beta)] \]

Similarly for the rural, it as follows,

\[ LL(\alpha, \beta|Data_r) \]
\[ = n_{r1} \ln[p(T = 1|\alpha, \beta)] + n_{r2} \ln[p(T = 2|\alpha, \beta)] + [n_u - (n_{r1} + n_{r2})] \ln[S(2|\alpha, \beta)] \]

After estimating the parameters the customer retention is calculated for the different discrete time period.
4.8 Findings and Analysis

Based on the methodology the different parameters are calculated using Microsoft Excel 2007. The survival data presented in table 4.1 are for segments of customer. One rural customer and another urban customer for grocery store type of business.

Table 4.1 Observed Percentage of Rural and Urban Customer

<table>
<thead>
<tr>
<th>Period</th>
<th>Rural Customer</th>
<th></th>
<th>Urban Customer</th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Alive (%)</td>
<td>Die (%)</td>
<td>Alive (%)</td>
<td>Die (%)</td>
</tr>
<tr>
<td>0 (First Purchase Occasion)</td>
<td>100</td>
<td>-</td>
<td>100.00</td>
<td>-</td>
</tr>
<tr>
<td>1 (Second Purchase Occasion)</td>
<td>74.48</td>
<td>23.68</td>
<td>55.37</td>
<td>44.63</td>
</tr>
<tr>
<td>2 (Third Purchase Occasion)</td>
<td>62.04</td>
<td>12.96</td>
<td>38.84</td>
<td>16.53</td>
</tr>
</tbody>
</table>

From Table 4.1 it is revealed that, in case of rural, 74.48 percent customers are alive in a grocery store in the second purchase occasion. It is assumed that the number of customer in first purchase occasion is considered as cohort of customer in particular store. In third purchase occasion, 62.04 percent customers are alive. It is also observed from table 4.1, that 23.68 percent and 12.96 percent customers are die (the customer is switched to another shop) in the second purchase occasion and third purchase occasion respectively. In case of urban, 55.37 percent and 38.84 percent customer is alive in urban grocery store in second purchase occasion and third purchase occasion respectively. Similarly,
44.63 percent and 16.53 percent customer is dying in the second purchase occasion and third purchase occasion respectively.

Now our approach is to fit the sBG model for the three purchase occasion of rural and urban customer. The following table gives the different value of the model parameters which is calculated using Microsoft Excel 2007.

**Table 4.2 Parameter Estimation**

<table>
<thead>
<tr>
<th>Places</th>
<th>( \hat{\alpha} )</th>
<th>( \hat{\beta} )</th>
<th>( \theta )</th>
</tr>
</thead>
<tbody>
<tr>
<td>Rural</td>
<td>0.559988</td>
<td>1.679963</td>
<td>0.25</td>
</tr>
<tr>
<td>Urban</td>
<td>0.901502</td>
<td>1.118529</td>
<td>0.446281</td>
</tr>
</tbody>
</table>

Table 4.2 gives the value of the model parameters and the churn probabilities of rural and urban customer. The churn probability of urban consumer is more than the rural consumer. This indicates that more rural customer is active with the same store than the urban customer. The urban customer is more chance to switch the other grocery store than the rural customer. It is clearer from the figure 4.2.
Figure 4.2 Distribution of Churn Probabilities for the Rural and urban Customer

From the figure 4.2 it is observed that the distribution of churn rate rural and urban customers is “reverse J-Shape”. These gives that within rural and urban customer have fairly low churn probabilities and follow the beta distribution. Closer examination shows that urban consumer has more churn rate than the rural consumer. After estimating the sBG model parameter the retention rate of each of
rural and urban consumer is computed the following table no 3 gives the customer retention rate of rural and urban for both the discrete time point second and third purchase occasion. Since, first purchase occasion is considered as cohort of customer for both rural and urban. The following table 3 gives the customer retention rate of rural and urban customer.

**Table 4.3 Customer Retention of Rural and Urban**

<table>
<thead>
<tr>
<th>Place</th>
<th>Purchase Occasion</th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Second</td>
<td>Third</td>
<td></td>
</tr>
<tr>
<td>Rural</td>
<td>0.75</td>
<td>0.827162</td>
<td></td>
</tr>
<tr>
<td>Urban</td>
<td>0.553719</td>
<td>0.701492</td>
<td></td>
</tr>
</tbody>
</table>

Table 4.3 shows that retention rate of rural customer is more than the urban customer in the second purchase occasion. Similarly, in the third purchase occasion rural customer has more retention rate than the urban customer. This indicates that rural customer has more chance to stay alive in the particular store than the urban customer. It is more comprehensible from the following graphical depiction.
Figure 4.3 Retention Rate of Rural and Urban Customer

4.9 Conclusion

The main purpose of the study is to compare the customer retention of rural and urban population. This study shows that customer retention of rural customers is greater than the urban customer. This means that rural customer is more attach with the same store than the urban customer at the different time horizon. This study also focuses the heterogeneity of customer at different time points. The urban consumer has more tendencies to leave the grocery store last purchase than the rural customer. The reason is that, (Vyas, 1997) it is observed that rural consumers vary not only in their behavior and practices but also in conviction and belief.